

Total Marks: 100

**MATHEMATICS (Part-1)**  
 (Fresh / New Course)

Time Allowed : 3 Hrs.

Marks: 20

**Section "A"**

Time : 20 Mins.

**NOTE :** Section-A is compulsory. All parts of this section to be answered on the questions paper itself. It should be completed in the given time and handed over to the Centre Superintendent. Deleting / Overwriting is not allowed. Do not use lead pencil.

**NOTE :** Insert the correct option (a, b, c, d) in the empty box opposite to each part.

Q. 1 Insert the correct option (a, b, c, d) in the empty box opposite to each part. Each part carries one mark.

- i) The matrix  $\begin{bmatrix} 2 & 0 \\ 0 & 2 \end{bmatrix}$  is called .....matrix. b
- (a) Diagonal (b) Scalar (c) Row (d) Null
- ii) The mid-point of the vectors (1, 2, 3) and (-1, -2, -3) is ..... b
- (a) (-1, -4, -9) (b) (0, 0, 0) (c)  $\left(\frac{-1}{2}, -2, \frac{-9}{2}\right)$  (d) (2, 4, 6)
- iii) If in a square matrix A,  $A^t = -A$ , then the matrix A is called .....matrix. c
- (a) Symmetric (b) Singular (c) Skew symmetric (d) Non singular
- iv) The  $\overline{AB}$  vector having the points A(-4, 6) and B(6, 8) then  $\overline{AB} =$  a
- (a)  $10i + 2j$  (b)  $10i - 2j$  (c)  $2i + 10j$  (d)  $-10i - 2j$
- v) If  $\vec{a}$  is any vector, then the unit vector  $\hat{a} =$  ..... b
- (a)  $\vec{a} \cdot |\vec{a}|$  (b)  $\frac{\vec{a}}{|\vec{a}|}$  (c)  $\frac{|\vec{a}|}{\vec{a}}$  (d)  $\vec{a} + |\vec{a}|$
- vi)  $\sum_{x=1}^4 (2x-3) =$  ..... b
- (a) 7 (b) 8 (c) 9 (d) 10
- vii) The general term of the Arithmetic sequence is  $a_n =$  ..... a
- (a)  $a + (n-1)d$  (b)  $a + (n+1)d$  (c)  $ar^{n+1}$  (d)  $ar^{n-1}$
- viii) For a geometric sequence with first term  $a_1$  and common ratio  $r = 1$ , then the sum of the first n term is  $S_n =$  ..... c
- (a)  $a_1 \left(\frac{1-r^n}{1-r}\right)$  (b)  $a_1 \left(\frac{r^n-1}{r}\right)$  (c)  $na_1$  (d)  $a_1 + (n-1)d$
- ix) How many different words can be formed from the letter "ABBAS"? a
- (a) 30 (b) 40 (c) 60 (d) 120
- x) If two events can not both occurs at the same time, they are called .....events. d
- (a) Simple (b) Equally likely (c) Compound (d) Mutually exclusive
- xi) The magnitude of the vector  $\vec{a} = 3i - j - k$  is ..... b
- (a)  $\sqrt{13}$  (b)  $\sqrt{11}$  (c)  $\sqrt{3}$  (d)  $\sqrt{5}$
- xii) If  $f(-x) = -f(x)$ , then the function f is called .....function. a
- (a) An odd (b) An even (c) An identity (d) A linear
- xiii)  $\cos(2\pi - \theta) =$  ..... c
- (a)  $-\cos\theta$  (b)  $-\sin\theta$  (c)  $\cos\theta$  (d)  $\sin\theta$
- xiv) If none of the angle of a triangle is right angle, then the triangle is called .....triangle. c
- (a) Single (b) Scalene (c) Oblique (d) Right angle
- xv) The general term of the binomial expression  $(a+b)^n$  is  $T_{r+1} =$  ..... a
- (a)  $\binom{n}{r} a^{n-r} b^r$  (b)  $\binom{n}{r} a^{r-n} b^r$  (c)  $\binom{r}{n} a^{r-n} b^n$  (d)  $\binom{n}{r} a^n b^{n-r}$
- xvi)  $1 - 2\sin^2 \theta =$  ..... a
- (a)  $\cos 2\theta$  (b)  $\sin 2\theta$  (c)  $2\cos 2\theta$  (d)  $2\sin 2\theta$
- xvii) A function has an inverse if and only if it is ..... a
- (a) 1-1 (b) Onto (c) 1-1 and onto (d) None of these
- xviii) In a right angled triangle one angle is ..... d
- (a)  $270^\circ$  (b)  $180^\circ$  (c)  $120^\circ$  (d)  $90^\circ$
- xix)  $2\pi$  is the period of ..... d
- (a)  $\operatorname{cosec}\theta$  (b)  $\cot\theta$  (c)  $\sec\theta$  (d) Both a and c
- xx) Real part of the complex number of the form  $(x-iy)^2$  is ..... a
- (a)  $x^2 - y^2$  (b)  $x^2 + y^2$  (c)  $x^2$  (d)  $y^2$

KT-XI-2016(A)  
**MATHEMATICS**  
 (Part - I)  
 (Old Course)

Time Allowed : 2:40 Hrs.

**Section - B**

Total Marks : 80  
 Marks : 50

**Q. 2** Write short answers of any TEN of the following parts. Each part carries equal marks.

- (i) Express  $1 + \sqrt{3}i$  in term of polar co-ordinates.
- (ii) Let  $S = \{0, 1, 2, 3, 4\}$ , draw the table which define a binary operation addition modulo 5.
- (iii) Find the remainder if  $f(x) = x^3 - 4x^2 + 2x$  is divided by  $x - 3$ .
- (iv) Decompose into partial fraction  $\frac{x^2 + 7}{(x^2 - 1)(x - 1)^2}$
- (v) Prove that  $C_r^n = C_{n-r}^n$
- (vi) Prove that  $1^2 + 2^2 + 3^2 + \dots + n^2 = \frac{n(n+1)(2n+1)}{6}$
- (vii) Prove that  $(\sec \theta - \tan \theta) = \frac{1 - \sin \theta}{1 + \sin \theta}$
- (viii) Sum the infinite series  $1 + \frac{3}{4} + \frac{7}{16} + \frac{15}{64} + \dots$
- (ix)  $\frac{\cos 75^\circ + \cos 15^\circ}{\sin 75^\circ - \sin 15^\circ} = \sqrt{3}$
- (x) Find the first three terms of the G.P when  $a_3 = \frac{9}{4}$  and  $a_6 = \frac{243}{256}$ .
- (xi) A die is thrown. What is the probability to get even number.
- (xii) For triangle ABC if  $a = 7, b = 5, c = 4$ . Find  $\beta$ .
- (xiii) Verify that  $\tan^{-1}\left(\frac{5}{6}\right) + \tan^{-1}\left(\frac{1}{11}\right) = \frac{\pi}{4}$

**Section - C**

Marks : 30

**NOTE :** Attempt any THREE questions. Each question carries equal marks.

**Q. 3** a) If  $\alpha, \beta$  are the roots of the equation  $mx^2 + nx + n = 0$  then prove that

$$\sqrt{\frac{\alpha}{\beta}} + \sqrt{\frac{\beta}{\alpha}} + \sqrt{\frac{n}{m}} = 0$$

(b) Find the coefficient of  $x^3$  in the expansion of  $\left(2x^2 + \frac{3}{x}\right)^{10}$

**Q. 4** a) Use Cramer's rule to solve

$$x - 2y + 4 = 0$$

$$3x + y + 5 = 0$$

$$2x + z + 1 = 0$$

b) Show that  $\sin 3\alpha = 3\sin \alpha - 4\sin^3 \alpha$

**Q. 5** a) Show by mathematical induction that  $\frac{5^n - 1}{24}$  is an integer.

b) Find  $S_8$  If  $S_5 = 175, a_{10} = 49$ .

**Q. 6** a) Solve the equation  $\sqrt{2x^2 + 3x - 15} + \sqrt{2x^2 + 3x + 1} = 32$

b) If  $\cot \theta = -1$  When  $-\pi \leq \theta \leq \pi$  find the other corresponding trigonometric ratios.