

ہال میں موبائل فون لانا بالکل منع ہے

Time Allowed : 3 Hrs.

MATHEMATICS
(Part - I)
(Fresh / New Course)

Total Marks: 100

NOTE : There are THREE sections in this paper i.e. Section A, B and C.

Time : 20 Mins.

Section "A"

Marks: 20

NOTE : Use this sheet for this section. No mark will be awarded for cutting, erasing or over writing.

Q. 1 Write the correct option i.e. A, B, C and D in the empty box provided opposite to each part.

- i) In order pair $i = \dots\dots\dots$ C (i)
(a) (1,0) (b) (-1,0) (c) (0,1) (d) (0,-1)
- ii) Let Z be a complex number, then $z \cdot \bar{z} = \dots\dots\dots$ a (ii)
(a) $|z|^2$ (b) $|z|$ (c) \sqrt{z} (d) $(z)^2$
- iii) A matrix in which the number of rows and number of column's are not equal, the matrix is called b (iii)
 $\dots\dots\dots$ matrix.
(a) Diagonal (b) Rectangular (c) Scalar (d) Square
- iv) In a square matrix A, $(A^{-1})^{-1} = \dots\dots\dots$ c (iv)
(a) $(A^{-1})^2$ (b) $(A^2)^{-1}$ (c) A (d) None of these
- v) A vector whose magnitude is one is called $\dots\dots\dots$ vector. b (v)
(a) Null (b) Unit (c) Zero (d) Equal
- vi) If $\vec{v} = 3i - 2j$ be a vector, then its magnitude is $|\vec{v}| = \dots\dots\dots$ a (vi)
(a) $\sqrt{13}$ (b) $\sqrt{5}$ (c) 1 (d) $\sqrt{-6}$
- vii) $i \times j = \dots\dots\dots$ c (vii)
(a) $(j \times i)$ (b) $(i \times k)$ (c) K (d) $(k \times j)$
- viii) The fourth term of a sequence $(-1)^{n-1} 2^{n+1}$ is $\dots\dots\dots$ b (viii)
(a) 32 (b) -32 (c) -16 (d) 16
- ix) The nth term of a geometric sequence is $a_n = \dots\dots\dots$ c (ix)
(a) $a + (n-1)d$ (b) $2a + (n-1)d$ (c) ar^{n-1} (d) ar^{n+1}
- x) If A, G and H be the A. Mean, G. Mean and H. Mean respectively, then $A \times H = \dots\dots\dots$ a (x)
(a) G^2 (b) \sqrt{G} (c) G (d) $(G)^{\frac{3}{2}}$
- xi) The factorial of zero is always equals to $\dots\dots\dots$ b (xi)
(a) Zero (b) One (c) Two (d) Three
- xii) How many different words can be formed from letter "BOOKKE"? a (xii)
(a) 180 (b) 120 (c) 90 (d) 360
- xiii) If A and B are mutually exclusive events, then $(A \cap B) = \dots\dots\dots$ set. c (xiii)
(a) Even numbers (b) Odd numbers (c) Empty (d) None of these
- xiv) If E be an event, then the range of $P(E)$ is ; a (xiv)
(a) $0 \leq P(E) \leq 1$ (b) $-1 \leq P(E) \leq 1$ (c) $1 \leq P(E) \leq 0$ (d) $1 \leq P(E) \leq 2$
- xv) If A and \bar{A} are the complementary events, then $P(\bar{A}) = \dots\dots\dots$ d (xv)
(a) $1 + P(A)$ (b) $\frac{1}{P(A)}$ (c) $P(A) - 1$ (d) $1 - P(A)$
- xvi) The nth term of $1.3 + 2.4 + 3.5 + \dots\dots\dots$ is $T_n = \dots\dots\dots$ b (xvi)
(a) $n(n+1)$ (b) $n(n+2)$ (c) $n(n+3)$ (d) $n(n-3)$
- xvii) Number of terms in the expansions of $(a+b)^{n+1}$ is $\dots\dots\dots$ d (xvii)
(a) n (b) $n + 1$ (c) $n - 1$ (d) $n + 2$
- xviii) When $f(-x) = -f(x)$, then the function $f(x)$ is called $\dots\dots\dots$ function. a (xviii)
(a) Odd (b) Even (c) Rational (d) Linear
- xix) $\cos(2\pi - \beta) = \dots\dots\dots$ b (xix)
(a) $-\cos\beta$ (b) $\cos\beta$ (c) $\sin\beta$ (d) $-\sin\beta$
- xx) $\cos\left(\frac{\theta}{2}\right) = \dots\dots\dots$ c (xx)
(a) $\sqrt{\frac{1 - \cos\theta}{2}}$ (b) $\sqrt{\frac{1 - \sin\theta}{2}}$ (c) $\sqrt{\frac{1 + \cos\theta}{2}}$ (d) $\sqrt{\frac{1 + \sin\theta}{2}}$

Time Allowed : 2:40 Hrs.

Section - B

Marks : 50

Q. 2 Answer any Ten parts. Each part carries equal marks.

- (i) Let $Z_1 = a + bi$ and $Z_2 = c + di$, then show that $\overline{Z_1 + Z_2} = \overline{Z_1} + \overline{Z_2}$.
- (ii) Factorize the polynomial $P(z) = z^3 - 2z^2 + z - 2$
- (iii) If $A = \begin{bmatrix} 3 & 2 \\ 4 & -1 \\ 6 & 1 \end{bmatrix}$ and $B = \begin{bmatrix} 2 & 5 \\ -1 & 4 \\ 0 & 3 \end{bmatrix}$, show that $(A+B)^t = A^t + B^t$.
- (iv) If A and B are the non-singular matrices, then show that $(AB)^{-1} = B^{-1}A^{-1}$.
- (v) Find the direction cosines of the vector from P(4, 8, -3) to Q(-1, 6, 2).
- (vi) Show that $k \cdot j \times i = -1$.
- (vii) Insert two geometric means between 64 and 125.
- (viii) Find the A. Mean, G. Mean and H. Mean for the numbers -6 and -216 and verify that $A \times H = G^2$.
- (ix) Find the sum of the series $2 + 5 + 10 + 17 + \dots$ to n terms.
- (x) Find n such that ${}^n P_5 = 9({}^{n-1} P_4)$.
- (xi) Show by mathematical induction that $5 + 10 + 15 + \dots + 5n = \frac{5n(n+1)}{2}$.
- (xii) If $f(x) = x^3 - 2$, then find $f^{-1}(3)$.
- (xiii) Show that $\tan\left(\frac{\pi}{2} + \theta\right) = -\cot \theta$

Section - C

Marks : 30

NOTE : Attempt any THREE questions. Each question carries equal marks.

Q. 3 (a) For what value of n will $\left(\frac{a^{n+1} + b^{n+1}}{a^n + b^n}\right)$ be the harmonic mean between "a" and "b".

(b) Show that $\begin{vmatrix} 1 & \alpha & \alpha^2 \\ 1 & \beta & \beta^2 \\ 1 & \gamma & \gamma^2 \end{vmatrix} = (\alpha - \beta)(\beta - \gamma)(\gamma - \alpha)$

Q. 4 (a) Show that $\left(\sin \frac{\alpha}{2} + \cos \frac{\alpha}{2}\right)^2 = 1 + \sin \alpha$

(b) Show that $\frac{1 + \cos 2\theta}{\sin 2\theta} = \cot \theta$

Q. 5 (a) Solve the triangle ABC by using the law of tangent, when $b = 12.5$, $c = 23$ and $\alpha = 38^\circ 20'$.

(b) Find the angle of the largest measure when $a = 7$, $b = 9$ and $c = 7$.

Q. 6 (a) Find the domain of the function $y = \operatorname{cosec} 2x$.

(b) Draw the graph of the function $y = \cos 2x$ when $0 \leq x \leq 2\pi$.