

0	0	0	0	0
1	1	1	1	1
2	2	2	2	2
3	3	3	3	3
4	4	4	4	4
5	5	5	5	5
6	6	6	6	6
7	7	7	7	7
8	8	8	8	8
9	9	9	9	9

2	3	4	7	2
0	0	0	0	0
1	1	1	1	1
2	2	2	2	2
3	3	3	3	3
4	4	4	4	4
5	5	5	5	5
6	6	6	6	6
7	7	7	7	7
8	8	8	8	8
9	9	9	9	9

MRD-XII-17 (A)
MATHEMATICS – (Part-II)
 (Fresh / New Course)

Total Time: 3hrs

Total Marks: 100



MAT12A

Time: 20min

"SECTION - A"

Marks: 20

Q. 1 Choose the correct option i.e. A,B,C, and D.

- i. If $f(x) = x^2$ then $f(x)$ is
 - (A) One-to-one
 - (B) Onto
 - (C) Many-to-one
 - (D) One-to-many
- ii. If $f(x) = x^2 - 4/x - 2$, then $f(2)$ is
 - (A) Zero
 - (B) Two
 - (C) Four
 - (D) Indeterminate
- iii. The slope of the secant line israte of change.
 - (A) Average
 - (B) Instantaneous
 - (C) Total
 - (D) No
- iv. If $y = e^x$, then the derivative of $y = e^x$ by first principal rule is
 - (A) 2
 - (B) 1
 - (C) 0
 - (D) -1
- v. The r 'th derivative of $f(x) = e^{mx}$ is
 - (A) $m^x e^{mx}$
 - (B) $m^r e^{mx}$
 - (C) $r^m e^{mx}$
 - (D) $x^m e^{mx}$
- vi. The Taylor series approximation of e^x equal the value of e^x for
 - (A) $x \in [-\infty, \infty]$
 - (B) $x \in (0, \infty)$
 - (C) $x \in (-1, 1)$
 - (D) $x \in (-1, 0)$
- vii. A portion of a graph that is cupped upward is called
 - (A) Concave down
 - (B) Concave up
 - (C) Point of inflection
 - (D) Both A & B
- viii. The relationship of calculus and vector methods is called
 - (A) Vector calculus
 - (B) Scalar calculus
 - (C) Vector
 - (D) Scalar
- ix. $\int \tan x dx =$
 - (A) $\log \cos x + c$
 - (B) $-\log \cos x + c$
 - (C) $-\ln |\cos x| + c$
 - (D) $\ln |\cos x| + c$
- x. To evaluate the integral $\int \sqrt{x^2 - 4} dx$ the process of integration is
 - (A) By parts
 - (B) By substitution
 - (C) By partial fraction
 - (D) By power rule
- xi. If $y = 2x + C$ then value of C for $x = 4$ and $y = 20$ is
 - (A) 20
 - (B) 12
 - (C) 8
 - (D) 4
- xii. The centroid of the triangle with vertices (3,-5), (-7, 4) and (10,-2) is
 - (A) (2, 1)
 - (B) (2, -1)
 - (C) (-2, 1)
 - (D) (-2, -1)
- xiii. The distance between the two points P (3,-2) and Q (-1,-5) is
 - (A) 25
 - (B) 5
 - (C) 49
 - (D) 9
- xiv. The circle equation with center C (0, 0) is
 - (A) $x^2 + y^2 = 4$
 - (B) $x + y = 4$
 - (C) $x^2 + y^2 = 4$
 - (D) $x^4 + y^4 = 4$
- xv. A point P(x_1, y_1) lies inside the circle $x^2 + y^2 = a^2$, if
 - (A) $x_1^2 + y_1^2 > a^2$
 - (B) $x_1^2 + y_1^2 \geq a^2$
 - (C) $x_1^2 + y_1^2 > a$
 - (D) $x_1^2 + y_1^2 \geq a$
- xvi. The parabola $y = ax^2 + bx + c$ opens upward if
 - (A) $a > 0$
 - (B) $b > 0$
 - (C) $c > 0$
 - (D) $y > 0$
- xvii. The focus of parabola $(x - h)^2 = 4p(y - k)$ is
 - (A) $F(h, k)$
 - (B) $F(h, k + p)$
 - (C) $F(h + p, k)$
 - (D) $F(h + p, k + p)$
- xviii. The relationship between the two sets of coordinate axes is called the of axes.
 - (A) Translation
 - (B) Rotation
 - (C) Transformation
 - (D) Both A & B
- xix. The differential equation $dy/dx = 1$ represents a family of straight lines which are
 - (A) Parallel
 - (B) Perpendicular
 - (C) Horizontal
 - (D) Vertical
- xx. If $f(x)$ is any continuous function of a single variable x then any number 'r' for which $f(r) = 0$ is called
 - (A) Root of $f(x)$
 - (B) Factor of $f(x)$
 - (C) Zero of $f(x)$
 - (D) Solution of $f(x)$

Time Allowed: 2:40 Hrs

Section – B & C
 “Section – B”

Total Marks: 80
 Marks: 50

Q. 2 Solve any TEN of the following parts. Each part carries equal marks.

- (i) Solve for x , $\log_b x = \frac{2}{3} \log_b 8 + \frac{1}{2} \log_b 9 - \log_b 6$
- (ii) Find $\frac{dy}{dx}$, if $y = \ln \sqrt{\frac{x+1}{x-1}}$
- (iii) Find the Maclaurin series expansion for the function $f(x) = \sin^2 x$
- (iv) If $\vec{v} = 2i - j + 5k$ and $\vec{w} = i + 2j - 3k$ then evaluate $\frac{d^2}{dt^2} = (t|\vec{v}| + t^2|\vec{w}|)$
- (v) Evaluate: $\int (\tan 3x + \sec 3x) dx$
- (vi) Evaluate: $\int \frac{\ln x}{x^3} dx$
- (vii) Find the angles of the triangle ABC whose vertices are A(3, -4), B(1, 5), C(2, -4)
- (viii) Find the equation of circle concentric to $2x^2 + 2y^2 + 16x - 7y = 0$ and is tangent to y-axis.
- (ix) Find the equation of set of all points with distance from (4, 3) that equal their distances from (-2, 1).
- (x) Translate to parallel axis through the point (3, -4) the conic $x^2 + 2y^2 - 6x + 16y + 39 = 0$
- (xi) Solve the homogeneous differential equation $\frac{dy}{dx} = \left(\frac{xy - y^2}{x^2} \right)$
- (xii) If $u = \tan^{-1} \left(\frac{x^2 + y^2}{x + y} \right)$ then show that $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} = \tan u$
- (xiii) Find the iterate x_3 of the Newton-Raphson iterative method for the function $f(x) = x^3 - 3$ with initial start $x_0 = 1$

“Section – C”

Marks: 30

NOTE: Attempt any three questions. Each question carries equal marks.

- Q. 3:**
 - a) Find $\frac{dy}{dx}$ where $y = \frac{1 + \tan 2x}{\operatorname{cosec} 3x}$
 - b) Find all the relative extrema of $f(x) = x^3 + 6x^2 + 9x + 2$
- Q. 4:**
 - a) Evaluate: $\int \sqrt{a^2 + x^2} dx$
 - b) Evaluate: $\int \frac{dx}{\sqrt{x}\sqrt{x^2 - 1}}$
- Q. 5:**
 - a) If A(0, 0), B(8, 6), C(12, 0) are the vertices of the triangle ABC, then show that the right bisectors of the sides of the triangle are concurrent.
 - b) The length of the tangent from (f, g) to the circle $x^2 + y^2 = 6$ is twice the length of the tangent to the circle $x^2 + y^2 + 3x + 3y = 0$, prove that $f^2 + g^2 + 4f + 4g + 2 = 0$
- Q. 6:**
 - a) For what value of 'C' the line $x + y + c = 0$ will touch the ellipse $\frac{x^2}{25} + \frac{y^2}{11} = 1$
 - b) Find the equation of hyperbola with vertices at (2, -2), (-4, -2) and passes through the point (5, 1)