

Mathematics Paper – XI (01) (19)



Name \_\_\_\_\_

1- اگر سوال کے ساتھ جارواڑا نہ دیجئے گئے، صرف صحیح جواب والوں کا نتیجہ پردازیں۔

Roll No. \_\_\_\_\_

2- درجون کو شیڈ (جہرے) کے لئے اپنے آئے رنگ کا رکار کرنے والا نتیجہ پردازیں۔

3- جواب میں ایک سے زائد رائج نہیں ہے جو اب غلط تصور ہو گا۔

Time Allowed: 20 Minutes

SECTION – A

Marks : 20

- 1 Period of  $\sec(3x)$  is.....   $\pi$   0   $2\pi$    $\frac{2\pi}{3}$
- 2 The graph of  $y = 2x^2 + 1$  is.....  Parabola  circle  straight line  None of these
- 3 The amplitude of  $5\sin(2x)$  is.....  1  -5  5  10
- 4 The inverse function of  $f(x) = \frac{x}{x-1}$  is...   $\frac{x-1}{x}$    $\frac{x+1}{x-1}$    $\frac{x}{1-x}$    $\frac{x}{x-1}$
- 5 When  $x = 5$ , then  $\frac{7! \times 6!}{x! \times (x+1)!} = \dots$   36  42  7  7!
- 6  $1 - x + x^2 - x^3 + \dots$  is the expansion of...   $(1-x)^{-2}$    $(1-x)^{-1}$    $(1+x)^{-2}$    $(1+x)^{-1}$
- 7 If  $c$  lies in the plane of  $a$  and  $b$ , then  $c = \dots$    $\alpha \vec{a} + \beta \vec{b}$    $\alpha \vec{a} \times \beta \vec{b}$    $\alpha \vec{a} \cdot \beta \vec{b}$   0
- 8 The domain of  $f(x) = \sqrt{x+1}$  is the set of all.....   $x > 0$    $x > 1$    $x \geq -1$    $x < -1$
- 9 The solution of linear inequality  $3x - 2 \geq 8 + 5x$  is.....   $[-\infty, -5]$    $(-\infty, -5]$    $[-\infty, 5)$    $[-\infty, -5]$
- 10 In right angled  $\triangle ABC$   $\alpha = 57^\circ$  then  $\beta = \dots$   57  90 $^\circ$   33'  33 $^\circ$
- 11 The multiplicative inverse of  $Z = 2 + 3i$  is.....   $2 - 3i$    $-2 - 3i$    $\frac{2}{13} - \frac{3}{13}i$    $\frac{2}{13} + \frac{3}{13}i$
- 12 Let  $A = \begin{bmatrix} 3 & -2 \\ 5 & 7 \end{bmatrix}$ . Then the co-factor of -2 is.....  -5  2  -2  5
- 13 The direction cosines of  $\vec{a} = 2\vec{i} - \vec{j} + \vec{k}$  are.....  2, 1, -1  2, -1, 1   $\frac{2}{\sqrt{6}}, \frac{1}{\sqrt{6}}, \frac{1}{\sqrt{6}}$    $\frac{2}{\sqrt{6}}, \frac{1}{\sqrt{6}}, \frac{1}{\sqrt{6}}$
- 14 Let  $A^2 = A$ , then  $\sum_{i=1}^3 A^i = \dots$   A  2A  A<sup>3</sup>  3A
- 15  $\sum_{k=1}^n k^2 = \dots$    $\frac{n(n+1)}{2}$    $\frac{n(n+1)(2n+1)}{6}$    $\left[\frac{n(n+1)}{2}\right]^2$   None of these
- 16 A fair die is rolled, the probability that even integer will occur is.....   $\frac{1}{2}$    $\frac{1}{3}$    $\frac{1}{4}$    $\frac{1}{6}$
- 17 The A.M between 6<sup>th</sup> and 8<sup>th</sup> term of the A.P 1, 4, 7, 10, ..... is.....  16  22  19  48
- 18 The vector perpendicular to  $-i + 2j + k$  and  $3i - k$  is.....   $5i - j - 3k$    $-5i - j - 3k$    $-5i + j + 3k$   None of these
- 19 If  $\frac{p}{q}$  is the third term of an H.P, then third term of corresponding A.P will be .. Coefficient of third term in the expansion
- 20 of  $\left(x + \frac{1}{2x}\right)^9$  is.....  7  14  56  9

Note: Time allowed for Section - B and Section - C is 2 Hours and 40 minutes.

**Section - B**

Marks: 50

**Q-II** Answer any TEN parts. Each part carries FIVE marks.

1. If  $Z_1 = 1 + 3i$ ,  $Z_2 = 2 + 3i$  evaluate  $\frac{|Z_1|}{|Z_2|}$
2. For what value of  $\lambda$  the homogeneous system  $x + 5y + 3z = 0$ ,  $5x + y - \lambda z = 0$ ,  $x + 2y + \lambda z = 0$  has non-trivial solution.
3. Solve the triangle for which  $a = 9$ ,  $b = 7$ ,  $c = 5$ .
4. Find the unit vector perpendicular to both  $\vec{a} = i + j + 2k$  and  $\vec{b} = -2i + j - 3k$
5. For a G.P  $a_{10} = \ell$ ,  $a_{13} = m$ ,  $a_{16} = n$  show that  $\ell n = m^2$
6. Given  $a_n = 201$  for the A.P 5, 9, 13, .... Find  $n$ .
7. Find the area of the inscribed circle of the triangle with measures of the sides 55m, 25m, 70m.
8. Solve for ' $n$ '  $n+1C_4 = 6 \cdot n-1C_2$
9. Prove by mathematical induction  $5 + 10 + 15 + \dots + 5n = \frac{5n(n+1)}{2}$
10. Find (without graphing) the vertex, intercepts and axis of  $f(x) = x^2 + 2x - 3$ .
11. Prove the identity  $\frac{\sin(\alpha) + \sin(9\alpha)}{\cos(\alpha) + \cos(9\alpha)} = \tan(5\alpha)$
12. Verify that  $(AB)^{-1} = B^{-1}A^{-1}$ , when  $A = \begin{bmatrix} 2 & 3 \\ 1 & 0 \end{bmatrix}$  and  $B = \begin{bmatrix} -1 & 1 \\ 2 & 3 \end{bmatrix}$
13. Graph  $y = -\cos(x)$  in  $0 \leq x \leq 2\pi$

**Section - C**

Marks: 30

Note : Attempt any THREE questions. Each question carries equal marks.

- Q-III** (a) Find the period, frequency, maximum and minimum value of the function  $y = 5 - 4 \sin(\theta + 30)$   
 (b) Show that  $\tan^{-1} \frac{3}{4} + \tan^{-1} \frac{8}{19} = \frac{\pi}{4}$

- Q-IV** (a) IF  $x^4$  and higher powers be neglected, then show that  $(1+x)^{\frac{1}{4}} + (1-x)^{\frac{1}{4}} = a - bx^2$ . Find also 'a' and 'b'.  
 (b) Show by mathematical induction that  $\frac{3^{2n} - 2^{2n}}{5}$  is an integer for all positive integers.

- Q-V** (a) Prove that  ${}^nC_r + {}^nC_{r-1} = {}^{n+1}C_r$   
 (b) What is the smallest angle of a triangle whose sides measure 25, 18 and 21 ft?

- Q-VI** (a) Solve the system of equation  $2x + 4y - z = 10$ ,  $x - 2y - 2z = -4$ ,  $3x + y + z = 7$  by Gauss elimination method.  
 (b) Show that  $f(x) = x \sqrt{x^2 + 3}$  is odd function.