

Note:

- 1) Attempting all MCQs is compulsory. This paper along with the OMR sheet must be returned to the superintendent after due time.
- 2) Fill the circle (A)(B)(C)(D), which one is correct with blue or black ball point, in this sheet as well as in separate OMR Sheet like ●
- 3) If more than one circle in the OMR sheet is filled then no credit will be given to such answer.

SECTION-A

1. $\frac{d}{dt}(\cot x) =$ _____
 (A) $\tan x \sec x$ (B) $-\cot x \operatorname{cosec} x$ ● $-\operatorname{cosec}^2 x$ (D) $\sec^2 x$
2. If $f(x, y) = \sin(x^2) \cos y$, then $\frac{\partial f}{\partial y} =$ _____
 (A) $2x \cos(x^2) \cos y$ (B) $\sin(x^2) \sin y$ (C) $2x \cos(x^2) \sin y$ ● $-\sin(x^2) \sin y$
3. The differential equation $\frac{dy}{dx} = \frac{f(x, y)}{g(x, y)}$ is homogenous if its degree is _____
 ● Positive (B) Negative (C) Zero (D) Constant
4. The order and degree of $\frac{d^2 y}{dx^2} + 2x \frac{dy}{dx} + y = 3$ is _____
 (A) 1, 1 (B) 1, 2 ● 2, 1 (D) 2, 2
5. $\int 5 dx =$ _____
 ● 5 (B) 10 (C) 15 (D) 20
6. $\int \frac{1}{x\sqrt{x^2 - a^2}} dx =$ _____
 ● $\frac{1}{a} \operatorname{sech}^{-1}\left(\frac{x}{a}\right) + c$ (B) $\frac{1}{a} \left| \sec^{-1}\left(\frac{a}{x}\right) \right| + c$ (C) $\frac{1}{a} \operatorname{sech}^{-1}\left|\frac{x}{a}\right| + c$ (D) $\frac{1}{a} \sec^{-1}\left|\frac{a}{x}\right| + c$
7. $\frac{d}{dt}(\vec{F} \times \vec{G}) =$ _____
 (A) $\frac{d\vec{F}}{dt} \times \vec{F} + \frac{d\vec{F}}{dt} \times \vec{G}$ (B) $\frac{d\vec{F}}{dt} \times \vec{G} + \frac{d\vec{G}}{dt} \times \vec{F}$ ● $\frac{d\vec{F}}{dt} \times \vec{G} + \vec{F} \times \frac{d\vec{G}}{dt}$ (D) $\vec{F} \times \frac{d\vec{F}}{dt} + \vec{G} \times \frac{d\vec{G}}{dt}$
8. The function $F(t) = (\sin t, (1-t)^t, \ln t)$ is continuous when _____
 ● $t > 0$ and $t \neq 1$ (B) $t \geq 0$ or $t \neq 1$ (C) $t \geq 0$ or $t = 1$ (D) $t \geq 0$ and $t \neq 1$
9. The point $P(c, f(c))$ for the function $f(x)$ is called critical point if _____
 (A) $f'(c) = 0$ or $f'(c)$ does not exist (B) $f'(c) = 0$ or $f'(c)$ exist ● $f'(c) = 0$ (D) $f'(c) \neq 0$
10. If $f(x) = \cos(ax + b)$ then $f''(x) =$ _____
 (A) $a^n \cos(ax + b)$ ● $a^n \cos\left(ax + b + \frac{n\pi}{2}\right)$ (C) $a^n \cos\left(ax + b - \frac{n\pi}{2}\right)$ (D) $a^n \cos\left(ax + \frac{n\pi}{2}\right)$
11. $\frac{d}{dx} (\operatorname{sech}^{-1} x) =$ _____
 (A) $\frac{-1}{x\sqrt{1-x^2}}$ (B) $\frac{1}{x\sqrt{1-x^2}}$ (C) $\frac{-1}{x\sqrt{x^2-1}}$ ● $\frac{1}{x\sqrt{x^2-1}}$
12. If $y = \sqrt{15x^2 + 1}$ then $\frac{dy}{dx} =$ _____
 (A) $\frac{x}{\sqrt{15x^2 + 1}}$ ● $\frac{15x}{\sqrt{15x^2 + 1}}$ (C) $\frac{\sqrt{15x^2 + 1}}{x}$ (D) $\frac{\sqrt{15x^2 + 1}}{15x}$
13. $\lim_{x \rightarrow 4} \left(\frac{\sqrt{x} - 2}{x - 4} \right) =$ _____
 (A) 4 ● $\frac{1}{4}$ (C) $\frac{1}{2}$ (D) 2

14. The function $f(x) = b^x$ decreases as x increases if _____
- (A) $b > 1$ (B) $1 < b < 2$ (C) $0 < b < 1$ (D) $0 > b > 1$
15. The direction cosines of the line perpendicular to $x - 5y + 3 = 0$ are _____
- (A) $\frac{-1}{\sqrt{26}}, \frac{5}{\sqrt{26}}$ (B) $\frac{1}{\sqrt{26}}, \frac{-5}{\sqrt{26}}$ (C) $\frac{-1}{\sqrt{26}}, \frac{-5}{\sqrt{26}}$ (D) $\frac{1}{\sqrt{26}}, \frac{5}{\sqrt{26}}$
16. The homogeneous equation, $ax^2 + 2hxy + by^2 = 0$ represent lines, which are real and distinct, if
- (A) $h = \sqrt{ab}$ (B) $h < \sqrt{ab}$ (C) $h > \sqrt{ab}$ (D) $h < \sqrt{ab}$
17. The equation of the circle passes through $(0, 0)$, whose intercepts on axes are 3 and 4 is _____
- (A) $x^2 + y^2 - 3x - 4y = 0$ (B) $x^2 + y^2 + 3x + 4y = 0$ (C) $x^2 + y^2 + 3x - 4y = 0$ (D) $x^2 + y^2 - 3x + 4y = 0$
18. The foci of ellipse $\frac{(x-h)^2}{a^2} + \frac{(y-k)^2}{b^2} = 1, a > b$ are _____
- (A) $F(h \pm c, k)$ (B) $F(h \pm c, -k)$ (C) $F(h + c, \pm k)$ (D) $F(h - c, \pm k)$
19. $x^2 + y^2 - 0$ is a parabola which opens _____
- (A) Upward (B) Downward (C) To the right (D) To the left
20. Equation of tangent to the circle $x^2 + y^2 = 25$ at point $(3, 4)$ is _____
- (A) $3x + 4y = 5$ (B) $4x + 3y = 5$ (C) $3x + 4y = 25$ (D) $4x + 3y = 25$

MATHEMATICS (Fresh) P-II

Note: Time allowed for section B and C is 2 hours and 40 minutes.

SECTION "B"

Marks: 40

II. Attempt any TEN Parts out of the following. Each Part carries equal marks.

- Evaluate the definite integral $\int_1^2 \frac{4}{t^3+4t} dt$
- Find the equation of straight line passing through the intersection of $2x-3y+4=0$ and $3x+4y-5=0$ and is perpendicular to the line $6x-7y-18=0$
- Evaluate $\lim_{x \rightarrow 5} \left(\frac{\sqrt{x}-\sqrt{5}}{x-5} \right)$.
- Differentiate $y = \ln \sqrt{\frac{x+1}{x-1}}$.
- Find the critical value of the function $f(x) = 2x^3 - 3x^2 - 72x + 15$.
- If $\vec{v} = 2\hat{i} - \hat{j} + 5\hat{k}$ and $\vec{w} = \hat{i} + 2\hat{j} - 3\hat{k}$ are two vector functions, then find the value of $\frac{d}{dt}(\vec{v} + t\vec{w})$.
- Evaluate $\int_4^9 \frac{dx}{4-x^2}$.
- Find the angle between the lines represented by $x^2 + xy + y^2 = 0$.
- Find the equation of tangents to the circle $x^2 + y^2 = 25$ which are parallel to the straight line $3x + 4y + 3 = 0$.
- Find the equation of parabola with line of symmetry is vertical, passes through $(-3, 4)$ and vertex at $v(5, 1)$.
- Solve the homogenous differential equation given by $\frac{dy}{dx} = \frac{xy - y^2}{x^2}$.
- Compute four iterates of the bisection method for $f(x) = x^2 - 10x + 23$, using intervals $[3.2, 4]$.
- Find the partial derivative's $f_x(x, y)$ and $f_y(x, y)$, where $f(x) = \sin^{-1}(xy)$.

SECTION "C"

Marks: 27

Note: Attempt any THREE questions of the following. Each question carries equal Marks.

- Use parametric differentiation to find $\frac{d^2y}{dx^2}$, where $x = a \cos 2t$ and $y = b \sin 2t$
 - Write the equation of the hyperbola with vertices $(2, -2)$ and $(-4, -2)$ and passes through $(5, 1)$.
- Evaluate the integral $\int \sin(2x) \ln(\cos x) dx$.
 - Find the equation of the circle that passes through $(0, 4)$, $(2, 6)$ and the line $x + y - 4 = 0$ is tangent to it at $(0, 4)$.
- Use the first principle rules to find $\frac{d}{dx}(a^x)$.
 - Indicate the centre, foci, ends of major and minor axes of $9(x-1)^2 + 16(y-2)^2 = 144$.
- Solve the initial value problem $y \frac{dy}{dx} + xy^2 = 0$
 - If $u = \tan^{-1} \left(\frac{x^2 + y^2}{x+y} \right)$, then show that $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} = \tan u$